O Experiment Total

The theoretical relationship for permanent enlargement ratio may be derived as follows. The enlargement of the bore under pressure is given by Eq. (21) substituting r = a. To find the permanent enlargement of the bore, the elastic recovery must be substracted from the enlargement under pressure. The elastic recovery is given by the Lamé equation and the value of pressure from  $\Gamma_{\uparrow\uparrow}$  (22).

The enlargement of the outside surface under internal pressure is found from Eq. (12), letting r-b and the elastic recovery of the exterior surface is again subtracted as was that for the inside surface. Dividing the resulting equation for permanent bore enlargement by that for permanent subtracted as the following equation for the permanent enlargement of the outside surface yields the following equation for the permanent enlargement ratio.

$$PER = \frac{1}{2} \left[ (2 - \mu) W + \frac{\mu}{W} \right] \tag{3}$$

A plot of this equation is shown in Fig. 10 for  $\mu = 0.3$ .

It is interesting to note that Eq. (25) can be derived directly from geometric considerations assuming no net change in volume as a result of overstrain.

## Percent Perman, at Rose Unlargement

From Fig. 9 it can be seen that, when a condition of 100 percent overstrain (strain factor = 1.0) is reached, the pressure-strain curve becomes essentially flat. It is, therefore, assumed that no additional benefit can be obtained by further deformation and then 100 percent overstrain is the optimum amount of deformation. Assure the higher diameter ratios where reverse yielding will occur to a bore on the release of the 100 percent overstrain pressure, the optime the optime there enlargement may be slightly less. However, in the diameter is investigated, this reverse yielding effect is considered negligible.

The position of the percent overstrain. These points are plotted in Fig. 11.

The theoretical curve shown is obtained by substituting r = a and  $\rho = b$  in Eq. (21) yielding the following equation for bore strain at 100 percent overstrain pressure.

$$\epsilon_{IWS} = \frac{a_{\theta}}{L} \left[ -1.08(1 - 2\mu) \ln W + \frac{\mu}{2} + \left(\frac{2 - \mu}{2}\right) W^2 \right]$$
(26)

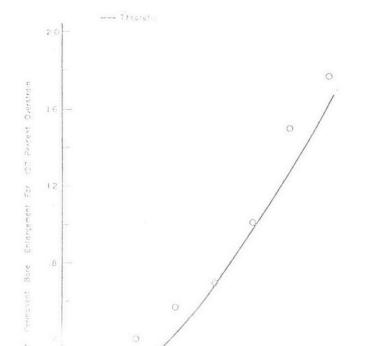


Fig. 11. Percent permanent bore enlargement for 100 per cent overstrain vs. diameter ratio.

Diometer Ratio

The elastic recovery at the bore is given by the Lamé equations and Eq. (4).

$$\epsilon_{lac} = \frac{\sigma_y}{E} \frac{1.08 \ln W}{W^2 - 1} \left[ (1 + \mu) W^2 + (1 - \mu) \right]$$
 (27)

165,000 psi Yield Strength

Subtracting Eq. (27) from Eq. (26) yields:

$$\epsilon_{taperm} = \left[\mu + (2 - \mu)H^2\right] \left[\frac{1}{2} - \frac{1.08 \ln H^2}{H^2 - 1}\right]$$
(28)

This equation is plotted in Fig. 11 for  $\mu = 0.3$  and is in good agreement with the experimental values.